UNIVERSITY OF CALIFORNIA, SANTA CRUZ BOARD OF STUDIES IN COMPUTER ENGINEERING



CMPE-242: Applied Feedback Control

HOMEWORK #6 Due 23-Feb-2017 @ 11:59PM

1. *Z-plane Root Locus*: Consider controlling the system G(s) with a discrete controller (in the usual unity feedback configuration) with a sample time of $\Delta T = 0.2$ sec:

$$G(s) = \frac{1}{s^2 + \frac{1}{5}s + 1}$$

- a. Use root locus techniques to design a compensator of the form $K(z) = \frac{K(z+a)}{z+b} \text{ that will yield closed loop roots in the z-plane that correspond to two poles at } s = -1. \text{ What is your } K(z)$?
- b. What is the DC gain of your closed loop system (work in the Z-domain)?
- c. Calculate the first three terms of the step response of your closed loop system. Do this by hand (i.e.: use long division), then use MATLAB's dstep to plot the step response as a check.

Note: there are an infinite number of controllers that will generate closed loop poles at the desired locations. If you have time, experiment with a few of these designs to get a feeling for working in the z-domain.

2. Discrete Bode: Consider the same system G(s) as before. This time the goal is to design a lead compensator using bode techniques (in the z-domain) that will yield an ω_{xo} = 5 rad/s with a phase margin of 36°:

$$G(s) = \frac{1}{s^2 + \frac{1}{5}s + 1}$$

a. What K(s) would work? (Place the pole and zero such that the peak phase of K(s) is at ω_{xo}).

- b. If $\Delta T = 0.2$, and K(z) = K (constant), what value of K will make the system go unstable? Sketch the Nyquist diagram.
- c. If $\Delta T = 0.01$, how much phase lead is necessary to meet the 36° phase margin spec? How much is necessary if $\Delta T = 0.2$?
- d. What K(z) will meet the specs if $\Delta T = 0.01$? Use dbode.m to plot the magnitude and phase of G(z)K(z).
- e. What K(z) will meet the specs if $\Delta T = 0.2$? Use dbode.m to plot the magnitude and phase of G(z)K(z).

Hint: Convert plant to G(z), then use gain to get ω_{xo} , from there, design your lead in s, and convert to K(z) using Tustin w/prewarping. Make sure to plot bode plots of both compensated and uncompensated plants.