

UNIVERSITY OF CALIFORNIA, SANTA CRUZ
 BOARD OF STUDIES IN COMPUTER ENGINEERING



CMPE-242:
 APPLIED FEEDBACK CONTROL

HOMWORK #9
 DUE 24-NOV-2010

1. Put the following transfer functions into state space using the controller canonical form (use MATLAB to check your answers after you have done them by hand):

a. $G(s) = \frac{2s+1}{s^2+3s+2}$

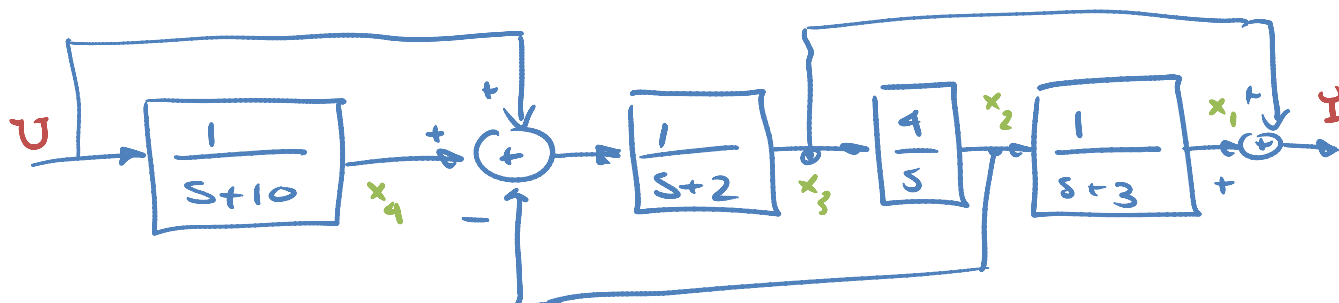
b. $G(s) = \frac{s+3}{s(s^2+2s+2)}$

c. $G(s) = \frac{3s+6}{2s+10}$ (hint: this one has a non-zero **D** term, use long division)

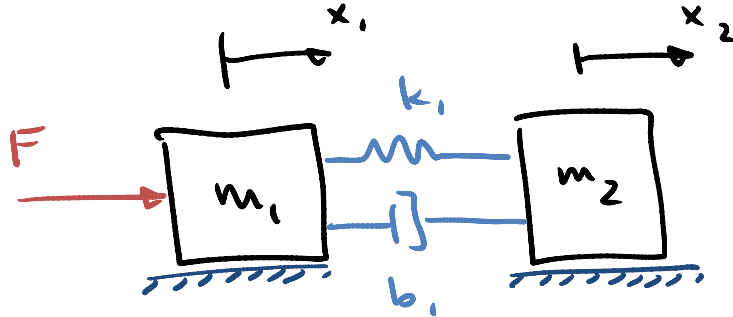
2. Given the following system, with zero initial conditions, find the steady state value of x to a step input:

$$\dot{x} = \begin{bmatrix} -8 & 2 \\ -4 & -2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

3. Write down the state equations using the states indicated in the drawing below, then derive the transfer function both using block diagram manipulation and linear algebra (and check that you get the same result):



4. Consider the following two mass problem that we have been looking at in class. Let the mass of the first mass be double the second mass: $m_1 = 2\text{Kg}$, $m_2 = 1\text{Kg}$, $k_1 = 0.5 \text{ N/m}$ and $b_1 = 0.05 \text{ Ns/m}$:



- Derive the state space equations using the state vector: $\mathbf{x} = [x_1 \quad \dot{x}_1 \quad x_2 \quad \dot{x}_2]^T$
- Find a similarity transform that will convert your answer in part (a) into a new set of equations with the state vector: $\mathbf{x}_{new} = [x_1 \quad \dot{x}_1 \quad x_{CM} \quad \dot{x}_{CM}]^T$, where x_{cm} refers to the center of mass of the two masses (remember to account for the different masses of m_1 and m_2).
 - What is the similarity transform: T and/or T^{-1}
 - What are the new state equations?
- Use MATLAB to plot the step response of the equations in both part (a) and (b), with the output being: $\mathbf{y} = [x_1 \quad x_{cm} \quad F]^T$
 - What are the two different \mathbf{C} and \mathbf{D} matrices?
 - Verify that both versions give the same response.
- Use ACKER.M and/or PLACE.M to design a full state feedback control law that will place the closed loop poles at $s = -1 \pm j$, $-2 \pm 2j$. Use the equations developed in part 4(b).
 - Derive the Controllability Matrix
 - Verify both the rank and the condition number of the Controllability Matrix.
 - What are your gains, K ?
 - Plot a step response of the system with the same output as in part (c).